



Frictional-anisotropy-based systems in biology: structural diversity and numerical model

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There is a huge variety in biological surfaces covered with micro- and nanostructures oriented at some angle to the supporting surface. Such structures, for example snake skin, burr-covered plant leaves, cleaning devices and many others cause mechanical anisotropy due to different friction or/and mechanical interlocking during sliding in contact with another surface in different directions. Such surfaces serve propulsion generation on the substrate (or within the substrate) for the purpose of locomotion or for transporting items. We have theoretically studied the dependence of anisotropic friction efficiency in these systems on (1) the slope of the surface structures, (2) rigidity of their joints, and (3) sliding speed. Based on the proposed model, we suggest the generalized optimal set of variables for maximizing functional efficiency of anisotropic systems of this type. Finally, we discuss the optimal set of such parameters from the perspective of biological systems.

Anisotropic surfaces are widespread in the non-biological world ranging from the molecular level¹ to the macroscopic level. The crystal structure of solids leads to the anisotropy of their surfaces on an atomic level. In engineering, anisotropy of certain texture patterns of polycrystalline materials is produced naturally or artificially during manufacturing of the materials. Surface anisotropy manifests itself even on geological scales where, due to tectonics, a majority of structures have well developed anisotropy.

There is also a huge variety in biological surfaces covered with micro- and nanostructures oriented at some angle to the supporting surface^{2–4}. Such structures cause mechanical anisotropy due to different friction or/and mechanical interlocking during sliding in contact with another surface in different directions. Such surfaces serve propulsion generation on the substrate (or within the substrate) for the purpose of locomotion or for transporting items. They have been previously described in a variety of mechanical systems belonging to different organisms ranging from the insect unguitactor plate^{5–9}, interlocking mechanisms of joints in insect legs and antennae³, insect ovipositor valvulae^{3,10–13}, animal attachment pads^{14–19}, inner surface of pitcher plants^{20–22}, wheat awns²³, fluids-guiding systems of plants²⁴, butterfly wings²⁵, etc.

The surface outgrowths, their joints to the supporting layer, and the supporting layer itself in most anisotropic surfaces in biology are rather rigid and rely on the ratchet principle in their mechanical behavior. However, some systems exhibit pronounced flexibility of surface structures due to the flexible material of the supporting layer or due to a specialized flexible joint connecting to the rigid supporting layer. A typical macroscale system of this kind is the snake skin consisting of rather stiff scales²⁶ embedded in a rather flexible supporting layer (Fig. 1). Preferred orientation of both scales themselves and surface microstructures has been discussed to be the key features responsible for the frictional anisotropy in this particular system^{27–30} (Fig. 2F). In addition, there is a microstructure at the level of the scale with strongly anisotropic orientation, which has been recently demonstrated to provide frictional anisotropy of the snake skin^{29,40} (Fig. 2G). Also shark skin exhibits a similar arrangement of stiff surface denticles embedded in a flexible collagenous supportive layer³¹. Another example has been reported from the burr-covered *Galium aparine* plant leaves/stems/fruits³², where burrs are connected to the supporting layer with a flexible joint³³. Cleaning devices of insects consist of rigid setae connected to the surface also with flexible joints^{34–36} (Fig. 3).

These numerous examples have a wide range of functions from the transport of particles (cleaning devices), the leaf positioning on the top of another leaf to the propulsion generation during slithering locomotion (snake). Since the rigidity of the support must have an influence on the mechanical behavior of these systems (as recently was shown for the snake skin⁴⁰), we have developed, in this paper, a model aiming at the study of their mechanical

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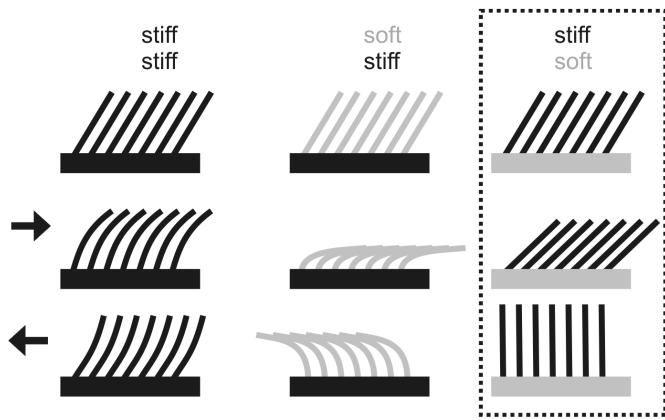


Figure 1 | Diagram of ratchet-like frictional anisotropic systems. First column, stiff protuberances on a stiff supporting layer. Second column, soft protuberances on a stiff supporting layer. Third column, stiff protuberances on a soft supporting layer. The third (framed) column indicates the system considered in the present study. First row, systems in non-deformed state. Second row, deformation caused by sliding in the direction of the protuberance slope. Third row, deformation caused by sliding in the direction opposite to the protuberance slope.

behavior (Fig. 4). We studied the dependence of the anisotropic friction efficiency on (1) the slope of the surface structures, (2) rigidity of their joints, and (3) sliding speed. Based on the proposed model, we suggest the generalized optimal set of variables for maximizing functional efficiency of anisotropic systems of this type. Finally, we discuss the optimal combination of such parameters from the perspective of biological systems.

Results

Typical time-dependencies of the friction force $F_{friction}(t)$ at positive $V > 0$ and negative $V < 0$ velocities are presented in the subplots (a) and (b) of Fig. 5, respectively. Bold lines in both cases show mean friction force

$$\langle F_{friction} \rangle = \frac{1}{t} \int_{t=0}^t F_{friction}(t), \quad (2)$$

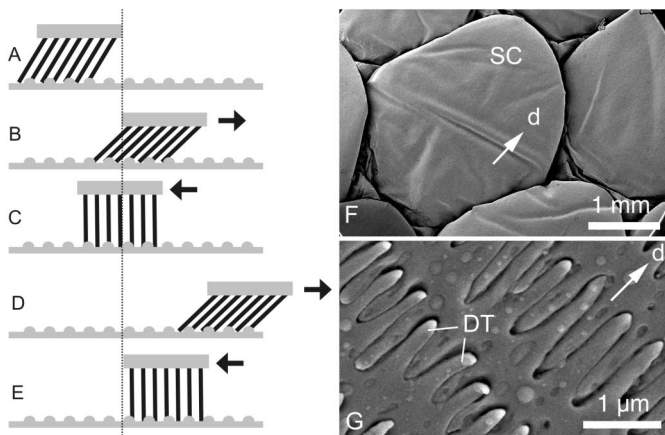


Figure 2 | System that assists body propulsion for locomotion. (A–E). Diagram showing how the soft-embedded sloped stiff array of protuberances can generate propulsion due to the opposite movements along a non-smooth substrate. (F, G). Lateral scales of the snake *Python regius* at different magnifications in the scanning electron microscope (SEM). d, direction toward the tail (caudal); DT, denticulations; SC, scales.

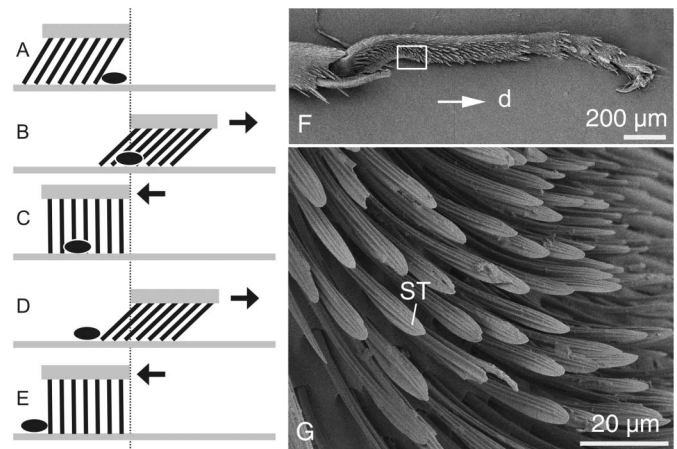


Figure 3 | System that generates particle movement for cleaning. (A–E). Diagram showing how the soft-embedded sloped stiff array of protuberances can generate unidirectional particle motion due to opposite movements along a substrate. (F, G). Foreleg of the ant *Formica polyctena* with a specialized cleaning device at different magnifications in SEM. d, distal direction; ST, setae.

accumulated from starting moment $t = 0$ to a current time t . Mean force $\langle F_{friction} \rangle$ averaged during sufficiently long time runs can be used to characterize the difference in system properties at varied elasticity K_β and velocities V . Results of numerical simulations performed at $V = \pm 1$ and varied K_β are presented in Fig. 6, where $\langle F_{friction} \rangle$ is shown in an interval of a few orders of amplitude $10^{-3} \leq K_\beta < 10^4$. A wide interval of K_β , where the system demonstrates strong anisotropy of the friction, is clearly seen. The optimal value of K_β is marked by a dash-dotted line. At a given set of the parameters it is around $K_\beta \simeq 1$.

It is important to note that the model is robust against particular choice of the elastic force $f_{elastic}(\beta)$. This force was chosen above as the linear function $f_{elastic} = K_\beta(\beta_0 - \beta)$, partially because we believe that this force monotonously increases with the deviation of the angle $\beta_0 - \beta$ from its equilibrium value, partially because to the moment we do not know its correct real dependence. An alternative choice could be $f_{elastic} = K_\beta \sin(\beta_0 - \beta)$ which reflects the fact that distortions of the skin $\delta l \sim \cos(\beta_0 - \beta)$ which tends as effective springs prevent a rotation of the fibers is proportional to the cosine: $\delta l \sim \cos(\beta_0 - \beta)$. Corresponding force $f_{elastic} = K_\beta \sin(\beta_0 - \beta)$ degenerates into linear one $f_{elastic} = K_\beta(\beta_0 - \beta)$ at small deviations $(\beta_0 - \beta) \rightarrow 0$. The results obtained in this variant of the model must coincide with the linear one in this limit. Stronger difference is expected in principle for large deviations, which can appear at negative velocities $V < 0$ and weak elastic constant $K_\beta \ll 1$, when external force is able to rotate fibers strongly. However, in this limit $f_{elastic} = K_\beta \sin(\beta_0 - \beta)$ also becomes nonrealistic too, because the force $f_{elastic}$ must grow monotonously at large deviations.

To compare two variants of the model, we performed numerical simulations with $f_{elastic} = K_\beta \sin(\beta_0 - \beta)$ also. The results are shown in Fig. 6 by dotted curve. As expected, a deviation is observable only for a combination of negative velocity $V < 0$ and weak elastic constant $K_\beta \ll 1$. For stronger $K_\beta \geq 1$ and for all positive velocities $V > 0$ two variants almost perfectly coincide (for positive V the difference is practically invisible in the figure). Let us account also, that majority of the results below will be obtained for the elastic constant close to the optimal value $K_\beta \simeq 1$. It allows limiting ourselves by the simplest linear model $f_{elastic} = K_\beta(\beta_0 - \beta)$. It is also important to admit that the present basic minimalistic model leaves outside the consideration of many important parameters, such as density and geometry of the stiff fibers, their length, thickness, etc, which may also affect the results. All these questions remain open for more specific further studies of

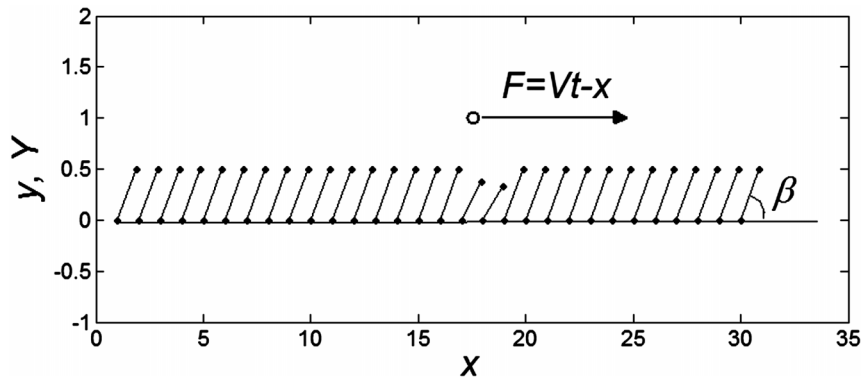


Figure 4 | Conceptual diagram of the model. The motion of the system is determined by Eq. (1) at equal damping constants $\gamma = \gamma_\beta = 1$, fixed elasticity $K = 1$ of external spring and interaction $f_0 = 1$ between the probe and hairs. Two other parameters: external velocity V and rigidity against rotations K_β remain varied.

concrete biological systems. The main advantage of the present model is in its simplicity and transparency both allowing considering the importance of the flexibility of structures for tuning of frictional anisotropy.

It is interesting also to study the inverse problem and apply friction anisotropy (which is, in fact, caused by real anisotropy of the interaction between the substrate and probe) to produce a directed drift of a “cargo”. To do this, let us put the probe on the top of the substrate and perform periodic oscillations of the substrate. One can check numerically that anisotropy of interaction really leads to a directed motion. We found directed drift even when a gently colored random noise of fluctuations with slightly preferable frequency Ω instead of strictly periodic oscillations is applied. Such sustainability against perturbations, and even ability of the system to produce directed motion at weakly pronounced preferences, must be extremely important for the biological applications of the effect. However, for the goals of this paper, below we limit ourselves to the strictly periodic oscillations with unique frequency Ω .

The numerical experiment in this case is as follows. We use the same Eq.(1), but change the external force to zero $K(Vt - x) = 0$. Instead, we move the substrate periodically and find out how the probe position changes during a sufficiently long run. Appearance of

the directed drift is characterized by a non-zero mean velocity $\langle V_x \rangle$:

$$\langle V_x \rangle = \frac{1}{t} \int_{t=0}^t V_x(t) dt \neq 0 \quad (3)$$

Figure 7 shows a dependence of mean drift velocity $\langle V_x \rangle$ on the K_β elastic constant at some representative frequencies Ω . The larger $\langle V_x \rangle$, the more pronounced the effect appears. Dot-dashed line in the figure corresponds to the optimal elasticity $K_\beta \approx 1$. At high frequencies curves $\langle V_x \rangle$ start to shift down monotonously. We do not show directly all the curves in order not to overload the figure. Instead, the direction of the shift is qualitatively marked by an arrow. One can collect optimal values of the drift velocity, found on each curve near $K_\beta \approx 1$, and plot them as a function of Ω . This is done in Fig. 8. Starting from a frequency slightly higher than $\Omega = 0.5$ (around $\Omega = 2\pi/10$ shown in Fig. 7) marked by a dash-dotted line, the drift exponentially goes down, especially at $\Omega \rightarrow \infty$. This exponential decay is clearly confirmed by the logarithmic plot in the insert to Fig. 8. At low frequencies $\Omega \leq 0.5$ drift velocity is almost constant. It means that at small frequencies $\Omega \leq 0.5$ the probe always has enough time to be captured by the substrate motion and tends to move much

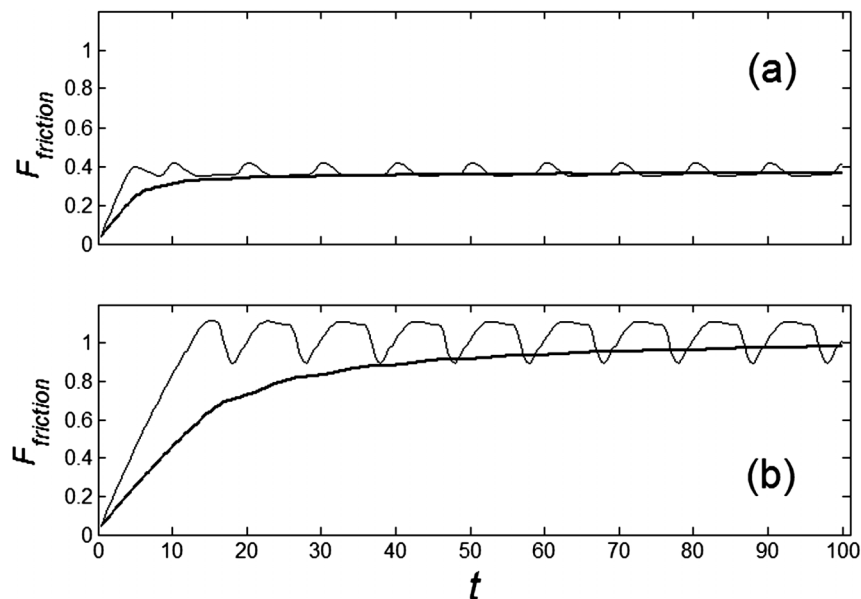


Figure 5 | Typical time dependencies of the friction force for positive $V > 0$ (a) and negative $V < 0$ (b) velocities. Bold lines in both cases show mean friction force ($F_{friction}$) averaged starting from $t = 0$ to a current moment of time t . The parameters are the same as in Fig. 4.

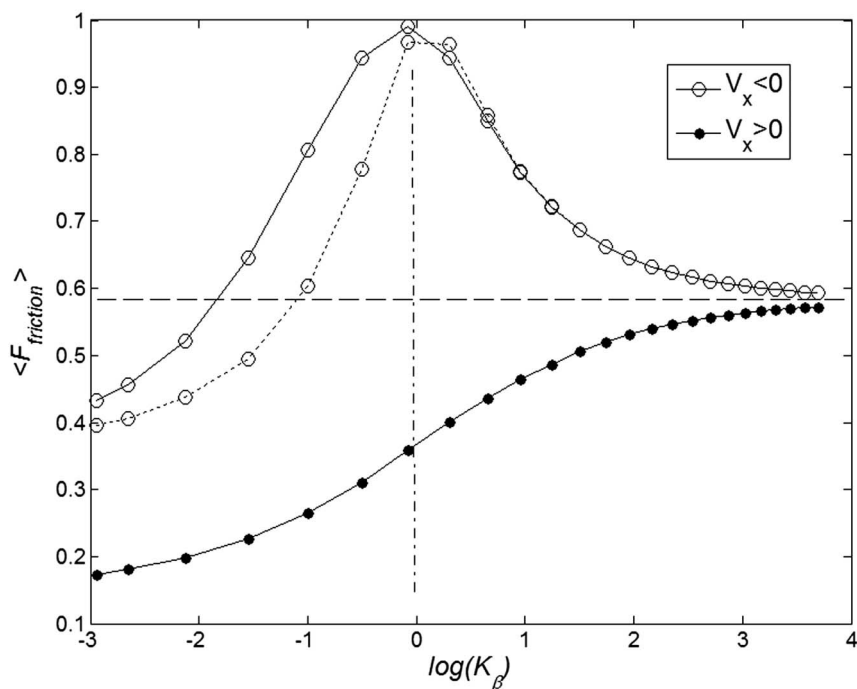


Figure 6 | Mean friction forces for fixed positive and negative velocities $V = \pm 1$ accumulated for a few orders of the absolute value $10^{-3} \leq K_\beta < 10^4$. Optimal elasticity around at $K_\beta \approx 1$, which corresponds to the maximal anisotropy of motion, is marked by dash-dotted line. To compare two variants of the model, numerical simulations with $f_{elastic} = K_\beta \sin(\beta_0 - \beta)$ also was performed (dotted curve).

more strongly in one preferred direction. From the practical point of view, one has also to count the time which every cycle of the motion lasts. This period is inversely proportional to the frequency $T \sim 1/\Omega$ and becomes very long for the extremely small $\Omega \rightarrow 0$. So, from the biological point of view, one can observe that frequency near the bending point (marked by the dash-dotted line) is an optimal case.

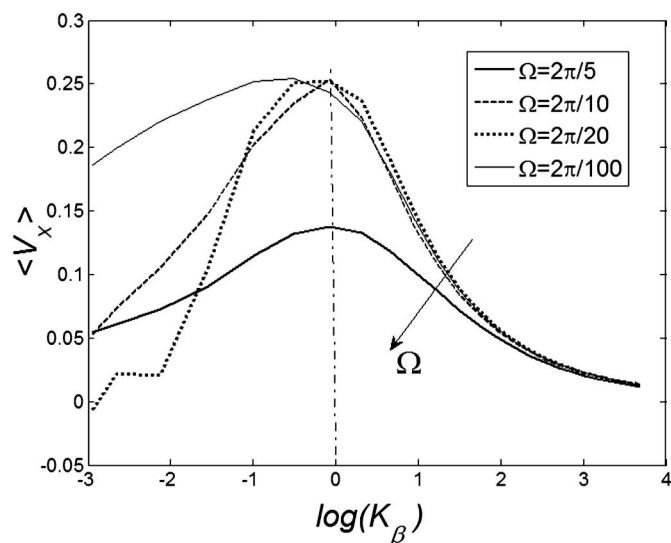


Figure 7 | Dependence of mean drift velocity $\langle V_x \rangle$ on the elasticity of the surface K_β calculated for some representative frequencies Ω . Dot-dashed line corresponds to optimal elasticity $K_\beta \approx 1$, at which the drift velocity is maximal. The arrow qualitatively marks monotonous shift of the curves $\langle V_x \rangle$ at frequencies higher than $\Omega = 2\pi/10$. Most of these curves (excluding one example for $\Omega = 2\pi/5$) are not shown here to do not overload the figure.

Discussion

The surprising not-trivial result of the study of the proposed model is that the degree of anisotropy, which is defined here as the relationship between forces, resisting sliding motion in both directions, is strongly dependent on the stiffness of the joints between individual sloped protuberances (hairs) and their supporting layer. Quite unexpectedly, the anisotropy is maximal at an intermediate stiffness of joints. Presumably, this is the reason why frictional systems, based on softly-embedded stiff sloped hairs, occur widely in biological mechanical devices dealing with propulsion/locomotion or transport of items/particles.

Another important conclusion from studying the model is that the degree of anisotropy depends on the frequency/velocity of sliding movements. There is a frequency at which the cumulative directed displacement, caused by oscillations in opposite directions, is maximal. The use of such a frequency in combination with particular stiffness of joints leads to an enhancement of the propulsive/carrying performance to several orders of magnitude.

One may assume that in biological evolution both oscillation frequency and joint stiffness were two important variables for the optimization of concrete mechanical systems. Performance of the systems requiring particular oscillating frequency for their proper functioning due to some other reasons, such as characteristic velocity of the muscle contraction, might be tuned to an optimum due to tuning of mechanical properties of hair joints. On the other hand, systems with constant mechanical properties of the joints might adapt their performance by tuning their specific oscillating frequency within the range of mathematically available frequencies. An optimal stiffness of joints is presumably comparable to specific forces at which the mechanical system usually operates. Stiff joints will not improve the performance at very low operating forces and, vice versa, soft joints will not maintain strong frictional anisotropy at very high forces.

Some biological anisotropic systems, such as snake skin, have an even higher degree of hierarchical organization of anisotropically-oriented structures (scales, denticulations) that may allow an

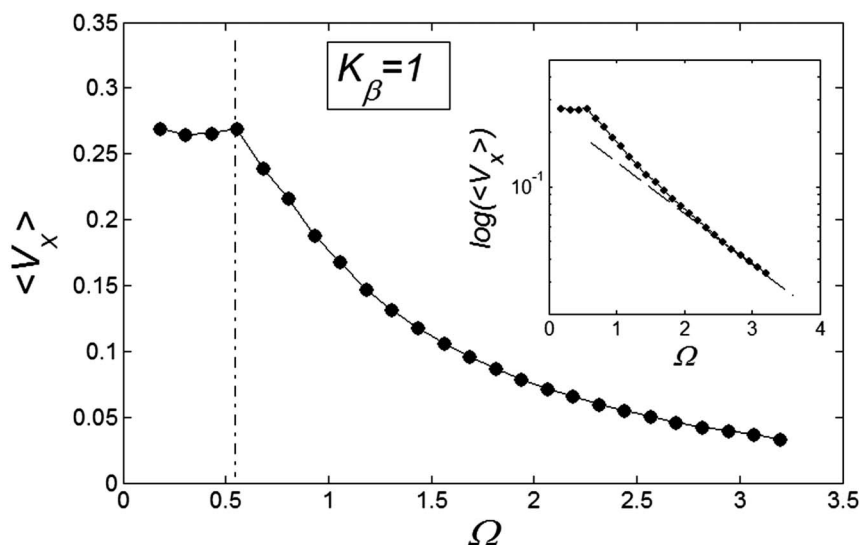


Figure 8 | Frequency dependence of drift velocity $\langle V_x \rangle$ calculated at fixed optimal elasticity $K_\beta \approx 1$. Logarithmic plot (inset) confirms an exponential decay of the drift velocity $\langle V_x \rangle$ at high Ω .

additional optimization of anisotropic frictional behavior at different macro- and microscopic levels of organization.

A very interesting observation of the behavior of the proposed model is that in the “cargo”-transporting devices, the transporting function completely fails at a certain minimal oscillating frequency. Nevertheless, both types of systems may properly operate at quite a wide range of joint stiffness and sliding velocities, which in biological evolution might be under the control of selective pressure. The model demonstrates an entire mathematical range of mechanical properties in combination with oscillating frequencies. However, in biological systems, spectra of these variables must be much narrower, because of limitations caused by specific biological factors. For example, biological systems cannot be too slow, if only because of the fact that a too long transport duration, even in an effective transporting process, might be too long compared with some specific physiological processes within a living organism or even compared with an organism’s length of life. On the other hand, the oscillating frequency cannot be too high, since the effectiveness of transport will decrease. Typical frequencies of sliding in various biological systems are in the range of 0.5–25 Hz and sliding velocity 0.01–50 m/s, and mutual relations between them are well within the range of the optimum predicted by the model.

Recently, biologically-inspired systems with anisotropic frictional properties have been developed³⁹. We believe that our model might aid in the further optimization of such systems for technological purposes. The verification of the model in different biological systems is not a simple task and it is currently in progress. Some preliminary results, showing the influence of the flexibility of supporting tissues on the degree of frictional anisotropy, are recently published⁴⁰. However, the verification of the model requires much broader range of parameters than that used in the above mentioned paper.

Methods

The present model explains the behavior of two different classes of mechanical functions of anisotropic surfaces with soft-embedded surface protuberances: propulsion/locomotion and transport of items/particles. In such systems, the interaction between the tips of protuberances and the substrate asperities or particles during a sliding motion effects the non-symmetric resistance of the anisotropic surface depending on (1) the direction of the movement and (2) orientation of hairs. However, this result is obvious and would be similar for other types of anisotropic surfaces with stiff or soft hairs embedded in the stiff matrix.

To construct a numerical model of the stiff hairs embedded in the soft matrix, we considered a simple configuration of the probe body connected to the spring, driven at fixed velocity V and interacting with 1-dimensional periodic array of stiff “hairs”.

The probe interacts with nearest hair with a force depending on an inclination angle β of the hair to the substrate plane: $f(\beta) = f_0 \sin(\beta) + const$. This force has a maximum $f(\beta) = f_0$ for the hair standing perpendicular to the surface and $f(\beta) \rightarrow const$ at $\beta \rightarrow 0$. A conceptual picture of the model is presented in Fig. 4. In real system, interaction between the probe and hair in horizontal orientation is much smaller than at nonzero angles $const \ll f_0$. Below, for the simplicity of the basic model, we will neglect this impact to the interaction and suppose that $f(\beta) \rightarrow 0$ at $\beta \rightarrow 0$.

At any moment of time t instant orientation of each hair depends on the relation between its place in the array x_j , $j = 1, 2, \dots, N$ and current position of the probe x . Normally the hair tends to keep angle $\beta \rightarrow \beta_0$ close to its equilibrium β_0 by an elastic force $f_{elastic} = K_\beta(\beta_0 - \beta)$. In biological structures, typical $K_{elastic}$ is in the range of 1–100 $\mu\text{N}/\text{rad}$. Instant inclination angle $\beta = \beta(x_j, t)$ is dynamically determined by a balance between pressure of the probe $f(\beta)$ and elastic force $f_{elastic} = K_\beta(\beta_0 - \beta)$. In turn, the probe detects a reaction of the hair $-f(\beta)$ and is driven by the external force $K(Vt - x)$. As a result one gets the following model equations:

$$\begin{aligned} \frac{\partial^2 x}{\partial t^2} &= K(Vt - x) - f(\beta) - \gamma \frac{\partial x}{\partial t}; \\ \frac{\partial \beta}{\partial t} &= \gamma_\beta^{-1} [f(\beta) + K_\beta(\beta_0 - \beta)], \end{aligned} \quad (1)$$

Here it is supposed that rotation of the hair inside a viscous substrate is strongly over-damped and material properties of the substrate are completely described by elastic K_β and damping γ_β constants. The value of damping γ_β of the substrate defines the characteristic time scale of the process and may be experimentally restored for a particular system. To study general properties of the model below, it is convenient to measure time in the units of γ_β^{-1} and take $\gamma_\beta = 1$. Preliminary study of the model shows that clearest manifestation of the friction anisotropy appears when damping of the external device is comparable to the internal one $\gamma \approx \gamma_\beta = 1$ and for the external elastic force $K\Delta x$ at typical elongation Δx close to one period of the structure $\Delta x \approx x_{j+1} - x_j = 1$ also comparable to the maximum $\max\{f(\beta)\} = f_0$ of interaction between the probe and hairs $K\Delta x \approx f_0$. Period of real structures in different biological systems has a wide range of dimensions (from 1 to 1000 μm), but typically 1–10 μm . So our unit of length corresponds to 1–10 μm . Below, for the sake of clarity, we will take that $K\Delta x = f_0 = 1$ and characterize the system by the remaining free parameters: relative elasticity $K_\beta/K \equiv K_\beta$ and external velocity V . The system of differential equations is simple enough to be easily solved numerically using any standard package of mathematical programs. In particular, we used MatLab program and applied time step $\Delta t = 10^{-4} \div 10^{-2}$, which is small enough to get stable behavior at the entire interval of variations of both parameters K_β and V .

Even before numerical solution one can intuitively predict that in the limiting case of extremely rigid $K_\beta \rightarrow \infty$ and extremely soft $K_\beta \rightarrow 0$ systems, the probe actually interacts either with almost fixed periodic substrate potential or with a practically flat surface, where the hair easily lays down under the influence of the external body sliding along the hair array. In both cases, the probe effectively interacts with static potential. Incline angle $\beta \rightarrow \beta_0$ may still make friction anisotropy possible, but one can expect that friction force weakly depends on the direction of motion and its values are very similar at positive $V > 0$ and negative $V < 0$ velocities. Another situation appears at some intermediate constant K_β , when the probe, moving against the inclination of the hairs $V < 0$, mounts them almost vertically, provoking strong resistance to the motion. In this case, resistance should essentially differ for two directions of motion. From the mathematical point of view it is an example of the movable systems providing directed transport due to anisotropic organization of the motion^{37,38}.



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Author contributions

Both authors have equally contributed to the manuscript.

Additional information

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